

UKS2 Calculation Policy

KEY STAGE 2

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

Key language: decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen. **Multiplication and division:** Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them.

Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

	Year 5					
	Concrete	Pictorial	Abstract			
Year 5 Addition						
Column addition with whole numbers	Use place value equipment to represent additions. TTh Th H T O O O O O O O O O O O O O O O O O O	Represent additions, using place value equipment on a place value grid alongside written methods. The the second	Use column addition, including exchanges. TTh Th H T O			
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving. FIG. 579 £28,370 £16,725	Use approximation to check whether answers are reasonable. TTh Th H T O 2 3 4 0 5 + 7 8 9 2 3 1 2 9 7			

	Adding tentl
	Adding decimals us
	column
	addition
п 1	

	Th	Н	Т	0
	2	6	0	0
+	1	4	5	0
	4	0	5	0
	1			

	Th	Н	Т	0
	2	6	0	0
+	4	0	5	0
	6	6	5	0

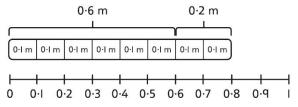
hs

Link measure with addition of decimals.

Two lengths of fencing are 0.6 m and 0·2 m.

How long are they when added together?

0.6 m 0.2 m Use a bar model with a number line to add tenths.



$$0.6 + 0.2 = 0.8$$

6 tenths + 2 tenths = 8 tenths

Understand the link with adding fractions.

$$\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$$

6 tenths + 2 tenths = 8 tenths

$$0.6 + 0.2 = 0.8$$

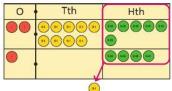
sing

Use place value equipment to represent additions.

Show 0.23 + 0.45 using place value counters.

Use place value equipment on a place value grid to represent additions.

Represent exchange where necessary.



	0	Tth	Hth
	2 (9	6
+	1 (0	4
	,		0
		1	_

Include examples where the numbers of decimal places are different.

0	Tth	Hth
00000		
•	01 01	

	0	Tth	Hth
	5 (0	0
+	1 (2	5
	6 '	2	5

Add using a column method, ensuring that children understand the link with place value.

	0	Tth	Hth
	0 (2	3
+	0 (4	5
	0 '	6	8

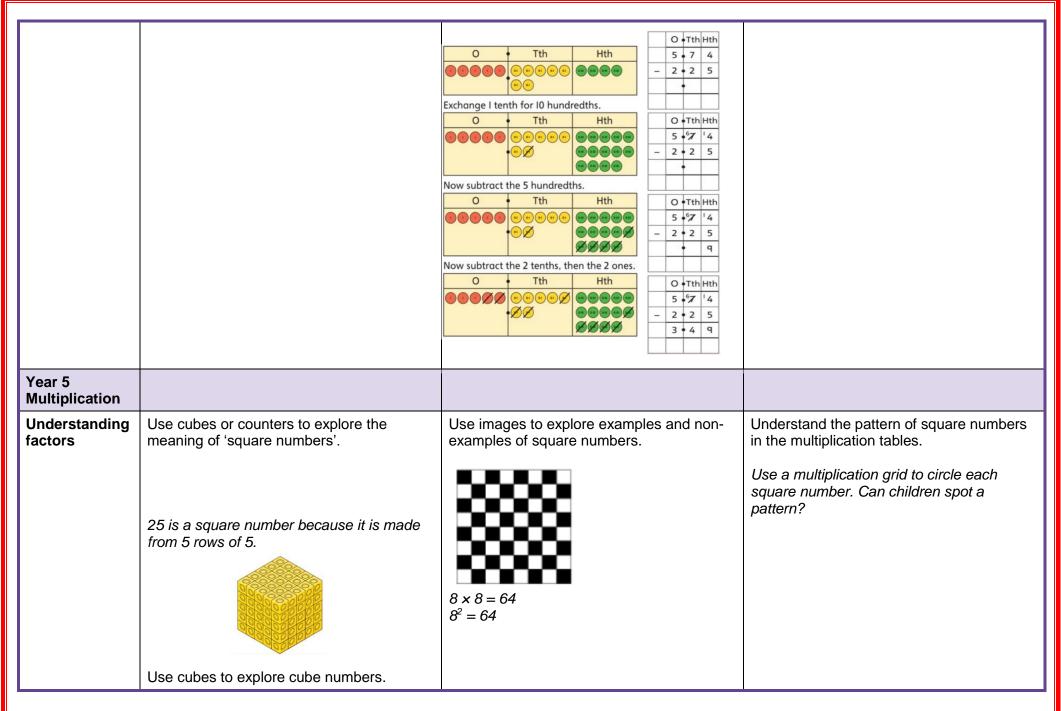
Include exchange where required, alongside an understanding of place value.

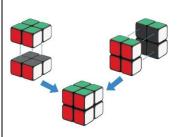
	0	Tth	Hth
	0 •	5	7
+	0 •	4	3
	1 4	0	0
	ı	ı	

			Include additions where the numbers of decimal places are different.
Year 5 Subtraction			
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. 2,250 – 1,070 = ?	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required. 15,735 - 2,582 = 13,153 The The Heart Operation of the calculation of the calcu	Use column subtraction methods with exchange where required. TTh Th H T O 58 2 5 9 7 - 1 8 0 3 4 4 4 5 6 3 62,597 - 18,034 = 44,563

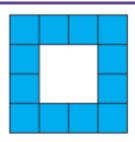
	TTh Th H T O I 5 7 3 5 - 2 5 8 2 TTh Th H T O I 5 6 7 3 5 - 2 5 8 2 5 3 TTh Th H T O I 5 6 7 3 5 - 2 5 8 2 I 3 I 5 3	
Checking strategies and representing subtractions	Bar models represent subtractions in problem contexts, including 'find the difference'. Athletics Stadium 75,450 Hockey Centre 42,300 Velodrome 15,735 ?	Children can explain the mistake made when the columns have not been ordered correctly. Use approximation to check calculations. Bella's working Correct method TTh Th H T O 1 7 8 7 7 + 4 0 1 2 5 7 9 9 7 I calculated 18,000 + 4,000 mentally to check my subtraction.

Choosing efficient methods			To subtract two large numbers that are close, children find the difference by counting on. 2,002 - 1,995 = ? 1,995 2,000 2,002 Use addition to check subtractions. I calculated 7,546 - 2,355 = 5,191. I will check using the inverse.
Subtracting decimals	Explore complements to a whole number by working in the context of length. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Use a place value grid to represent the stages of column subtraction, including exchanges where required. 5.74 - 2.25 = ?	Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places. 2.000 - 0.296 = ? O Tth Hth Thth





8 is a cube number.



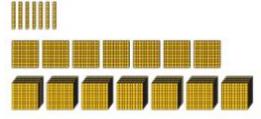
12 is not a square number, because you cannot multiply a whole number by itself to make 12.

Multiplying by 10, 100 and 1,000

Use place value equipment to multiply by 10, 100 and 1,000 by unitising.

$4 \times 1 = 4$ ones = 4	8	8	6
4 × 10 = 4 tens = 40			 annon
4 × 100 = 4 hundreds = 400			

Understand the effect of repeated multiplication by 10.

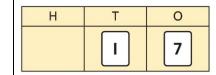


 $7 \times 10 = 70$

 $7 \times 100 = 7,000$

 $7 \times 1,000 = 70,000$

Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.



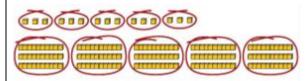
 $17 \times 10 = 170$

 $17 \times 100 = 17 \times 10 \times 10 = 1,700$

 $17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000$

Multiplying by multiples of 10, 100 and 1,000

Use place value equipment to explore multiplying by unitising.



5 groups of 3 ones is 15 ones. 5 groups of 3 tens is 15 tens. Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.



 $4 \times 3 = 12$ $4 \times 300 = 1,200$



 $6 \times 4 = 24$ $6 \times 400 = 2,400$ Use known facts and unitising to multiply.

$$5 \times 4 = 20$$

 $5 \times 40 = 200$
 $5 \times 400 = 2,000$
 $5 \times 4,000 - 20,000$

 $5,000 \times 4 = 20,000$

	So, I know that 5 groups of 3 thousands would be 15 thousands.		
Multiplying up to 4-digit numbers by a single digit	Explore how to use partitioning to multiply efficiently. $8 \times 17 = ?$ $8 \times 10 = 80$ $8 \times 10 = 80$ $8 \times 7 = 56$ $80 + 56 = 136$ So, $8 \times 17 = 136$	Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 100s, then 1,000s. H T O O O O O O O O O O O O O O O O O	Use an area model and then add the parts. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Multiplying 2- digit numbers by 2-digit numbers	Partition one number into 10s and 1s, then add the parts. $23 \times 15 = ?$ $10 \times 15 = 150$ $1 $	Use an area model and add the parts. $28 \times 15 = ?$ 10 m $20 \times 10 = 200 \text{ m}^2$ 5 m $20 \times 5 = 100 \text{ m}^2$ $8 \times 10 = 80 \text{ m}^2$ $8 \times 5 = 40 \text{ m}^2$	Use column multiplication, ensuring understanding of place value at each stage. $\begin{array}{ c c c c c c c c c c c c c c c c c c c$

	23 × 15 = 345		
Multiplying up to 4-digits by 2-digits		Use the area model then add the parts. 100	Use column multiplication, ensuring understanding of place value at each stage. Th H T O

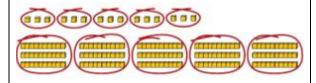
First multiply I,274 by 2.

Multiplying decimals by 10, 100 and 1,000	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid. i) $0.14 \times 10 = \boxed{}$ $0.14 \times 10 = \boxed{}$ $0.14 \times 10 = 1.4$	Understand how this exchange is represented on a place value chart. The Heat Tool Tth 2.5 × 10 = 25 2.5 × 100 = 250 2.5 × 1,000 = 2,500 The Heat Tool Tth 2.5 × 100 = 250 2.5 × 1,000 = 2,500
Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number. $24 \div 3 = 8$ $24 \div 8 = 3$ 8 and 3 are factors of 24 because they divide 24 exactly. $24 \div 5 = 4$ remainder 4.	Understand that prime numbers are numbers with exactly two factors. $13 \div 1 = 13$ $13 \div 2 = 6 r 1$ $13 \div 4 = 4 r 1$ 1 and 13 are the only factors of 13. 13 is a prime number.	Understand how to recognise prime and composite numbers. I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder. I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33. I know that 1 is not a prime number, as it has only 1 factor.

	5 is not a factor of 24 because there is a remainder.		
Understanding inverse operations and the link with multiplication, grouping and sharing	Use equipment to group and share and to explore the calculations that are present. I have 28 counters. I made 7 groups of 4. There are 28 in total. I have 28 in total. I shared them equally into 7 groups. There are 4 in each group. I have 28 in total. I made groups of 4. There are 7 equal groups.	Represent multiplicative relationships and explore the families of division facts. $60 \div 4 = 15$ $60 \div 15 = 4$	Represent the different multiplicative relationships to solve problems requiring inverse operations. 2 ÷ 3 =
Dividing whole numbers by 10, 100 and 1,000	Use place value equipment to support unitising for division. $4,000 \div 1,000$ $4,000 \times 1,000 \times 1,000$	Use a bar model to support dividing by unitising. $380 \div 10 = 38$ 380 380 380 380 380 380 380	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000. The Head Toology The Toolo

Dividing by
multiples of 10,
100 and 1,000

Use place value equipment to represent known facts and unitising.



15 ones put into groups of 3 ones. There are 5 groups.

$$15 \div 3 = 5$$

15 tens put into groups of 3 tens. There are 5 groups.

$$150 \div 30 = 5$$

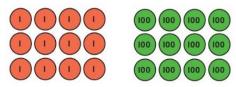
Represent related facts with place value equipment when dividing by unitising.



180 is 18 tens.

18 tens divided into groups of 3 tens. There are 6 groups.

$$180 \div 30 = 6$$



12 ones divided into groups of 4. There are 3 groups.

12 hundreds divided into groups of 4 hundreds. There are 3 groups.

$$1200 \div 400 = 3$$

Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.

$$3,000 \div 5 = 600$$

 $3,000 \div 50 = 60$
 $3,000 \div 500 = 6$

$$5 \times 600 = 3,000$$

 $50 \times 60 = 3,000$
 $500 \times 6 = 3,000$

Dividing up to four digits by a single digit using short division

Explore grouping using place value equipment.

$$268 \div 2 = ?$$

There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones.

$$264 \div 2 = 134$$

Use place value equipment on a place value grid alongside short division.

The model uses grouping.

A sharing model can also be used, although the model would need adapting.

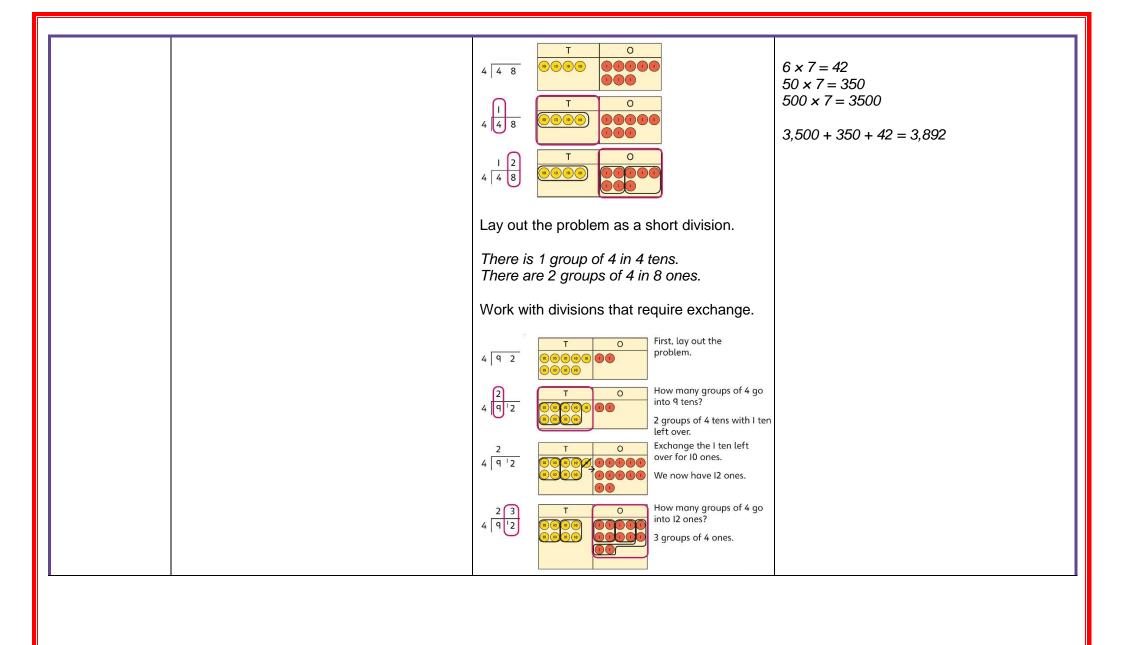
Use short division for up to 4-digit numbers divided by a single digit.

	0	5	5	6	
7	3	³ 8	3 q	⁴ 2	

$$3.892 \div 7 = 556$$

Use multiplication to check.

$$556 \times 7 = ?$$



Understanding remainders

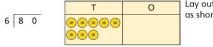
Understand remainders using concrete versions of a problem.

80 cakes divided into trays of 6.

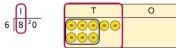


80 cakes in total. They make 13 groups of 6, with 2 remaining.

Use short division and understand remainders as the last remaining 1s.



Lay out the problem as short division.



How many groups of 6 go into 8 tens?

There is I group of 6 tens.

There are 2 tens remaining.

How many groups of 6 go into 20 ones?

There are 3 groups of 6 ones.

There are 2 ones remaining.

In problem solving contexts, represent divisions including remainders with a bar model.

		683			
136	136	136	136	136	3

$$683 = 136 \times 5 + 3$$

 $683 \div 5 = 136 \, r \, 3$

Dividing decimals by 10, 100 and 1,000

Understand division by 10 using exchange.

2 ones are 20 tenths.

20 tenths divided by 10 is 2 tenths.

Represent division using exchange on a place value grid.

T	0	Tth	Hth
000	00		
T	0 (Tth	Hth
		<u> </u>	
	000		
		00 00	
		<u></u>	
	888	000	

32 is 3 tens and 2 ones.

This is equivalent to 30 ones and 20 tenths.

30 ones divided by 10 is 3 ones.

20 tenths divided by 10 is 2 tenths.

32 divided by 10 is 3.2.

Understand the movement of digits on a place value grid.

0	Tth	Hth	Thth
0,	8_	5_	
0	0/2	×8 /	\searrow_5

$$0.85 \div 10 = 0.085$$

0 •	Tth	Hth	Thth
8 💐	_5~	/	
0 •	0	→ 8	→ 5

$$8.5 \div 100 = 0.085$$

Understanding the relationship between fractions and division

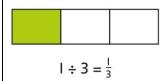
Use sharing to explore the link between fractions and division.

1 whole shared between 3 people. Each person receives one-third.





Use a bar model and other fraction representations to show the link between fractions and division.

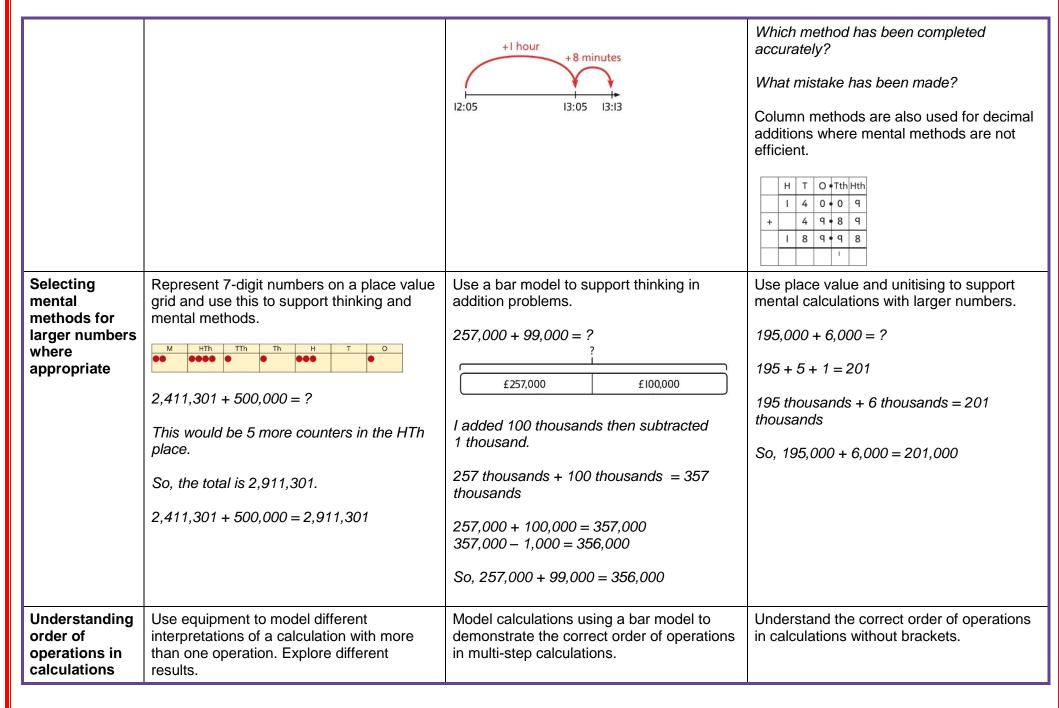


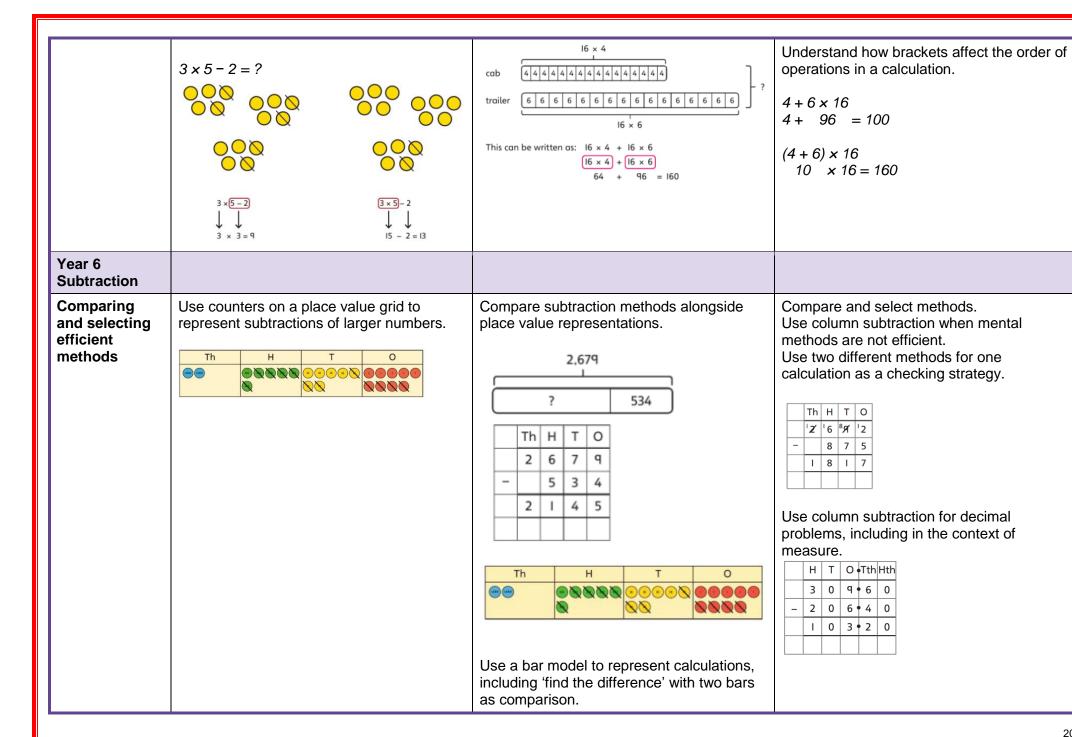
Use the link between division and fractions to calculate divisions.

$$5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$$

$$11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$$

Year 6								
	Concrete	Pictorial	Abstract					
Year 6 Addition								
Comparing and selecting efficient methods	Represent 7-digit numbers on a place value grid and use this to support thinking and mental methods.	Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations. TTh Th H T 0 4 0 3 6 5 + 3 5 7 2	Use column addition where mental methods are not efficient. Recognise common errors with column addition. 17,877 + 4,012 = ?					





		$ \begin{array}{c} \text{computer game} \\ \text{puzzle book} & \\ & \\ \text{£12.50} \end{array} $	
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. 950,000 - 150,000 That is 950 thousands - 150 thousands	Subtract efficiently from powers of 10. $10,000 - 500 = ?$
Year 6 Multiplication		So, the difference is 800 thousands. 950,000 - 150,000 = 800,000	
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications. Th T O O O O O O O O O O O O O O O O O O	Use place value equipment to compare methods. Method I	Understand area model and short multiplication. Compare and select appropriate methods for specific multiplications. Method 3 3,000 200 20 5 4 12,000 800 80 20 12,000 + 800 + 80 + 20 = 12,900 Method 4 1 2 9 0 0

Multiplying up to a 4-digit number by a 2-digit number

Use an area model alongside written multiplication.

4,200 + 630 + 105 = 4,935

	200	30	5
20	4,000	600	100
- 1	200	30	5

		2	3	5	
×			2	1	
				5	1 × 5
			3	0	I × 30
		2	0	0	I × 200
		1	0	0	20 × 5
		6	0	0	20 × 30
	4	0	0	0	20 × 300
	4	q	3	5	21 × 235

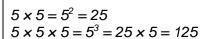
Use compact column multiplication with understanding of place value at all stages.

		2	3	5	
×			2	1	
		2	3	5	I × 235
	4	7,	0	0	20 × 235
	4	q	3	5	21 × 235

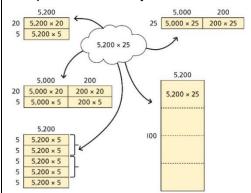
Using knowledge of factors and partitions to compare methods for multiplications

Use equipment to understand square numbers and cube numbers.



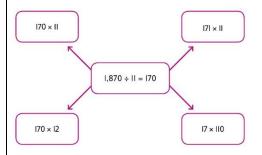


Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.



Represent and compare methods using a bar model.

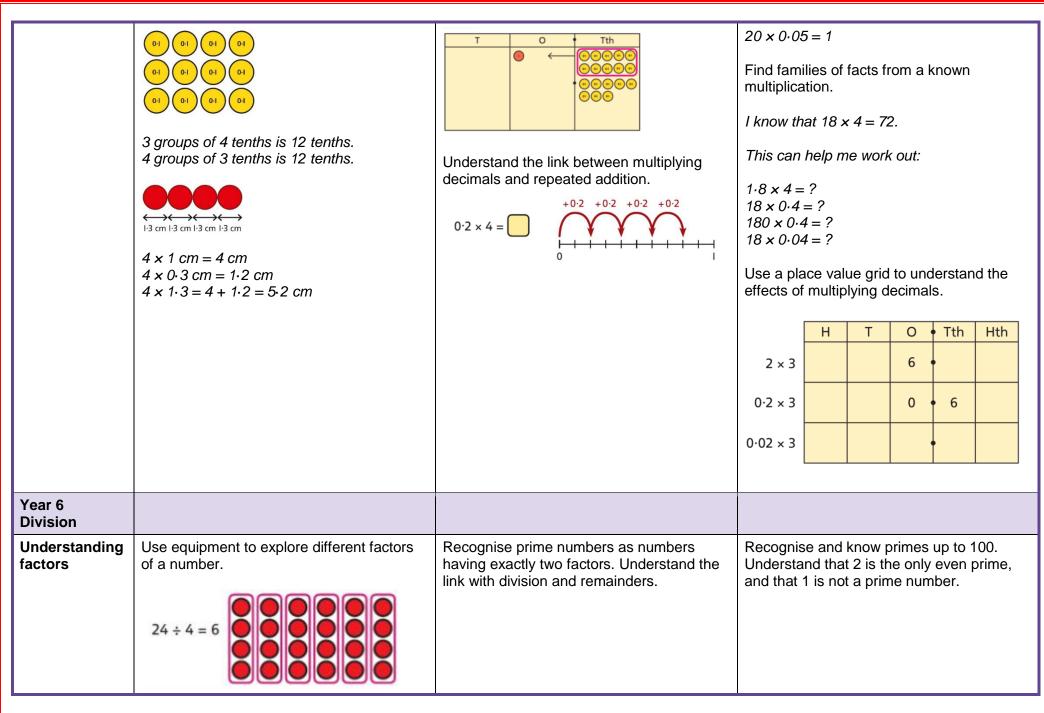
Use a known fact to generate families of related facts.

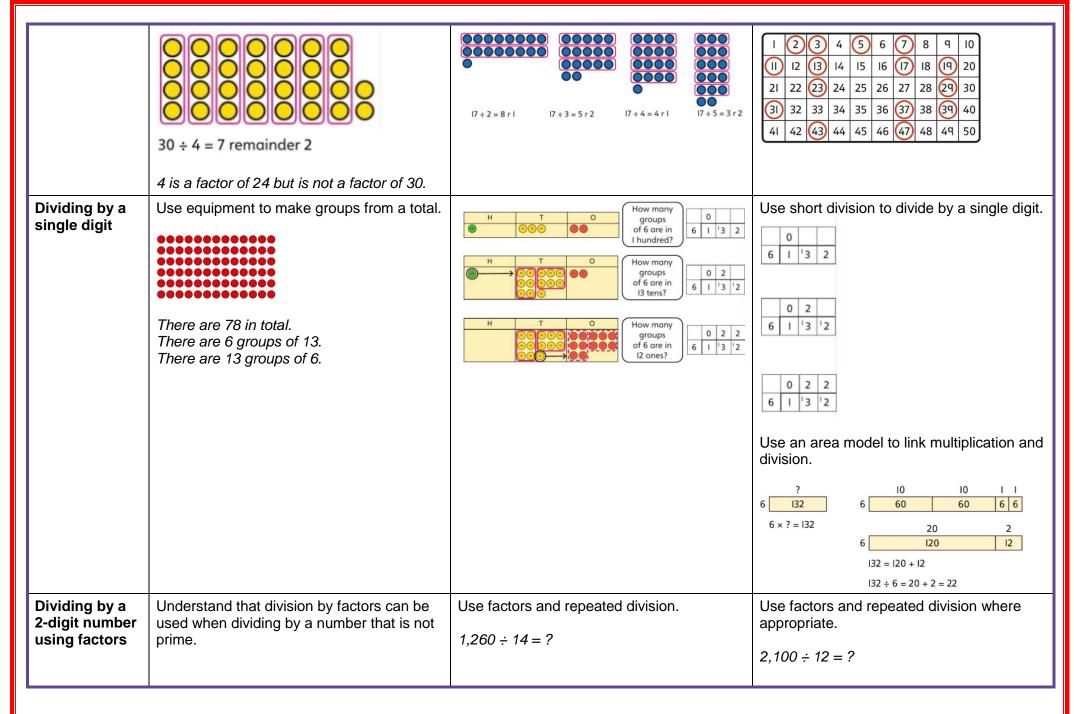


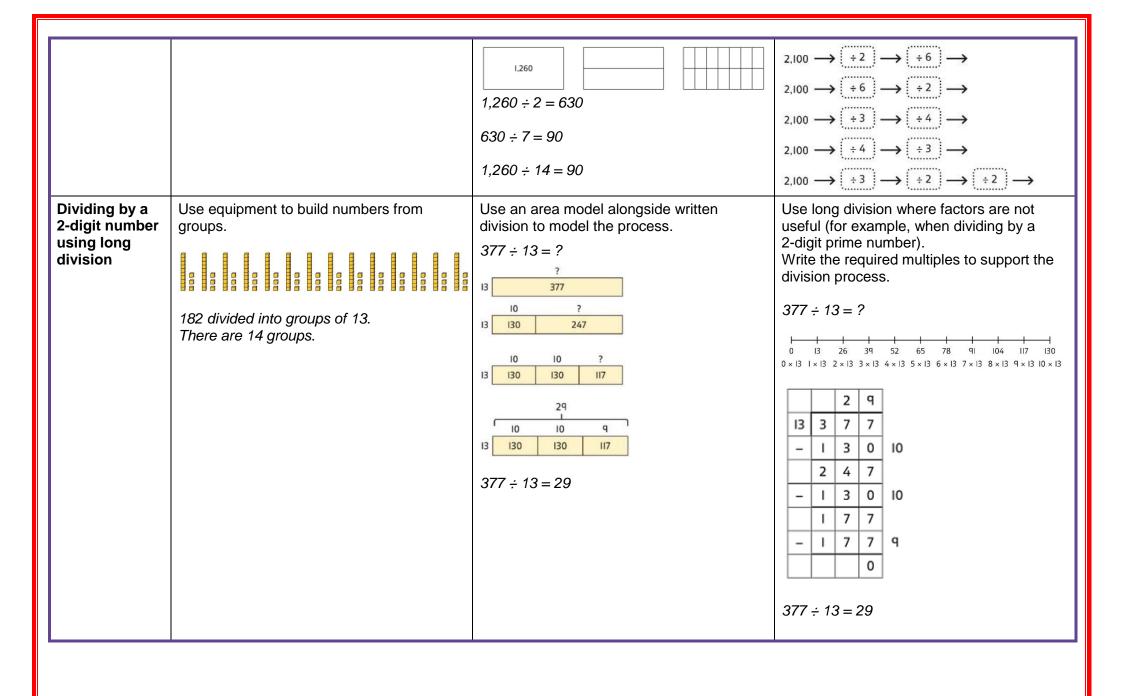
Use factors to calculate efficiently.

$$15 \times 16$$
$$= 3 \times 5 \times 2 \times 8$$

			$= 3 \times 8 \times 2 \times 5 = 24 \times 10 = 240$
Multiplying by 10, 100 and 1,000	Use place value equipment to explore exchange in decimal multiplication. 0·3 × 10 = ? 0·3 is 3 tenths. 10 × 3 tenths are 30 tenths. 30 tenths are equivalent to 3 ones. T O Tth Represent 0·3. T O Tth Represent 0·3. Exchange each group of ten-tenths.	Understand how the exchange affects decimal numbers on a place value grid. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000. $8 \times 100 = 800$ $8 \times 300 = 800 \times 3$ $= 2,400$ $2.5 \times 10 = 25$ $2.5 \times 20 = 2.5 \times 10 \times 2$ $= 50$
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures.	Represent calculations on a place value grid. $6 \times 3 = 18$ $6 \times 0.3 = 1.8$	Use known facts to multiply decimals. $4 \times 3 = 12$ $4 \times 0.3 = 1.2$ $4 \times 0.03 = 0.12$ $20 \times 5 = 100$ $20 \times 0.5 = 10$







			A slightly different layout may be used, with the division completed above rather than at the side. 3 21 7 9 8 - 6 3 0 1 6 8 21 7 9 8 - 6 3 0 1 6 8 - 1 6 8 0 Divisions with a remainder explored in problem-solving contexts.
Dividing by 10, 100 and 1,000	Use place value equipment to explore division as exchange. Output Divide 20 counters by 10. Output Exchange each 0-1 for ten 0-01s. Divide 20 counters by 10. Output Divide 20 counters by 10. Output Divide 20 counters by 10.	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use knowledge of factors to divide by multiples of 10, 100 and 1,000. $40 \rightarrow \begin{array}{c} \div 10 \\ \hline \\ 40 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ 40 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ 40 \rightarrow \end{array} ?$ $40 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ 40 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ \hline \\ 8 \rightarrow 10 = 0.8 \\ \hline \\ 80, 40 \rightarrow 50 = 0.8 \\ \hline \\ 10 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ 10 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ \\ \\ 10 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ \\ \\ 10 \rightarrow \begin{array}{c} \div 5 \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$

Dividing decimals

Use place value equipment to explore division of decimals.



8 tenths divided into 4 groups. 2 tenths in each group.

Use a bar model to represent divisions.

0.8				
?	?	?	?	

 $4 \times 2 = 8$

$$8 \div 4 = 2$$

So,
$$4 \times 0.2 = 0.8$$
 $0.8 \div 4 = 0.2$

Use short division to divide decimals with up to 2 decimal places.